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> restart;

with(plots);

unprotect( $\gamma$ );

Digits := 20;

c := 299792458;

 $\lambda$  := 1.310E-6;

NumberOfLoops := 15;
BendRadius := 0.015;
SingleLoopWidth := 2 · BendRadius;
SingleLoopLength := 0.304;
TotalArmLength := NumberOfLoops · SingleLoopLength;
TotalArmWidth := NumberOfLoops · SingleLoopWidth;
TotalFiberLengthPerArm := evalf(NumberOfLoops · 2 · (SingleLoopLength +  $\pi$  · BendRadius));

Altitude := 23 ·  $\frac{\pi}{180}$ ;

vWind := 420000;

v := evalf(vWind · abs(cos(Altitude)));

n1 := 1.44915;
n2 := 1.44975;

n := n2;

 $\gamma := \text{evalf}\left(\frac{1}{\text{sqrt}\left(1 - \left(\frac{v}{c}\right)^2\right)}\right)$ ;

cn :=  $\frac{c}{n}$ ;

FractionOfTimeLightIsHeldByMolecules :=  $\frac{(n-1)}{n}$ ;

TimeLightIsHeldByMolecules :=  $\gamma$  · FractionOfTimeLightIsHeldByMolecules ·  $\frac{L}{cn}$ ;

t0 :=  $\frac{L}{cn}$ ;

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$$L1 := \text{sqrt}(L^2 + (\text{abs}(v) \cdot dtDiagonal - \text{abs}(v) \cdot TimeLightIsHeldByMolecules)^2);$$

$$Eqdt0 := dtDiagonal = t0 + \left( \frac{L1 - L}{c} \right);$$

$$\theta := '\theta';$$

$$unitXcomponent := \text{abs}(\cos(\theta)^2);$$

$$unitYcomponent := \text{abs}(\sin(\theta)^2);$$

$$TotalArmLengthA := unitXcomponent \cdot TotalArmLength;$$

$$TotalArmWidthA := unitYcomponent \cdot TotalArmWidth;$$

$$TotalArmLengthB := unitYcomponent \cdot TotalArmLength;$$

$$TotalArmWidthB := unitXcomponent \cdot TotalArmWidth;$$

$$L := TotalArmLengthA;$$

$$dtTotalArmLengthA := \text{solve}(Eqdt0, dtDiagonal)_1;$$

$$L := TotalArmWidthA;$$

$$dtTotalArmWidthA := \text{solve}(Eqdt0, dtDiagonal)_1;$$

$$L := TotalArmLengthB;$$

$$dtTotalArmLengthB := \text{solve}(Eqdt0, dtDiagonal)_1;$$

$$L := TotalArmWidthB;$$

$$dtTotalArmWidthB := \text{solve}(Eqdt0, dtDiagonal)_1;$$

$$dtPerpendicularArm1 := 2 \cdot (dtTotalArmLengthA + dtTotalArmWidthA);$$

$$dtPerpendicularArm2 := 2 \cdot (dtTotalArmLengthB + dtTotalArmWidthB);$$

$$L := 'L';$$

$$\begin{aligned}
TotalArmLengthContractedA &:= \frac{unitYcomponent \cdot TotalArmLength}{\gamma}; \\
TotalArmWidthContractedA &:= \frac{unitXcomponent \cdot TotalArmWidth}{\gamma}; \\
TotalArmLengthContractedB &:= \frac{unitXcomponent \cdot TotalArmLength}{\gamma}; \\
TotalArmWidthContractedB &:= \frac{unitYcomponent \cdot TotalArmWidth}{\gamma};
\end{aligned}$$

$$\begin{aligned}
dtParallelArm1 &:= \frac{TotalArmLengthContractedA + TotalArmWidthContractedA}{(c + v)} \\
&+ \frac{TotalArmLengthContractedA + TotalArmWidthContractedA}{\frac{(c - v)}{n}};
\end{aligned}$$

$$\begin{aligned}
dtParallelArm2 &:= \frac{TotalArmLengthContractedB + TotalArmWidthContractedB}{(c + v)} \\
&+ \frac{TotalArmLengthContractedB + TotalArmWidthContractedB}{\frac{(c - v)}{n}};
\end{aligned}$$

$$dtArm1 := (dtPerpendicularArm1 + dtParallelArm1);$$

$$dtArm2 := (dtPerpendicularArm2 + dtParallelArm2);$$

$$dxArm1 := dtArm1 \cdot c;$$

$$dxArm2 := dtArm2 \cdot c;$$

$$d\theta_{arm1} := \frac{dxArm1}{\lambda} \cdot 2 \cdot \pi;$$

$$d\theta_{arm2} := \frac{dxArm2}{\lambda} \cdot 2 \cdot \pi;$$

$$LightIntensityEnvelope := 2 \cdot \sin(d\theta_{arm1} - d\theta_{arm2});$$

$$WaveArm1 := \sin(d\theta_{arm1});$$

$$WaveArm2 := \sin(d\theta_{arm2});$$

$$LightIntensity := WaveArm1 + WaveArm2;$$

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TimeDifference :=  $\frac{\text{Shift} \cdot \lambda}{c}$ ;
dtEq := TimeDifference = dtArm1 - dtArm2;

FringeShift := evalf(solve(dtEq, Shift));

plot0 := plot(FringeShift,  $\theta = 0 \dots 2\pi$ , view = [0 .. 2 $\pi$ , -5 .. 5]);

plot1a := plot(LightIntensityEnvelope,  $\theta = 0 \dots 2\pi$ , view = [0 .. 2 $\pi$ , -10 .. 10]);
plot1b := plot(LightIntensityEnvelope,  $\theta = 0 \dots 2\pi$ , view = [0 .. 2 $\pi$ , -10 .. 10]);

plot2 := plot(LightIntensityEnvelope,  $\theta = 0 \dots \frac{\pi}{2}$ , view = [0 ..  $\frac{\pi}{2}$ , -10 .. 10]);
plot3 := plot(LightIntensityEnvelope,  $\theta = 260 \cdot \frac{\pi}{180} \dots 360 \cdot \frac{\pi}{180}$ , view = [260 ·  $\frac{\pi}{180}$  .. 360 ·  $\frac{\pi}{180}$ , -10 .. 10]);

plot4 := plot(FringeShift,  $\theta = 225 \cdot \frac{\pi}{180} \dots 325 \cdot \frac{\pi}{180}$ , view = [225 ·  $\frac{\pi}{180}$  .. 325 ·  $\frac{\pi}{180}$ , -5 .. 5]);

display([plot0]);
display([plot1a]);
display([plot1b]);
display([plot2]);
display([plot3]);
display([plot4]);

```

[[animate](#), [animate3d](#), [animatecurve](#), [arrow](#), [changecoords](#), [complexplot](#), [complexplot3d](#), [conformal](#), [conformal3d](#), [contourplot](#), [contourplot3d](#), [coordplot](#), [coordplot3d](#), [densityplot](#), [display](#), [dualaxisplot](#), [fieldplot](#), [fieldplot3d](#), [gradplot](#), [gradplot3d](#), [implicitplot](#), [implicitplot3d](#), [inequal](#), [interactive](#), [interactiveparams](#), [intersectplot](#), [listcontplot](#), [listcontplot3d](#), [listdensityplot](#), [listplot](#), [listplot3d](#), [loglogplot](#), [logplot](#), [matrixplot](#), [multiple](#), [odeplot](#), [pareto](#), [plotcompare](#), [pointplot](#), [pointplot3d](#), [polarplot](#), [polygonplot](#), [polygonplot3d](#), [polyhedra\\_supported](#), [polyhedraplot](#), [rootlocus](#), [semilogplot](#), [setcolors](#), [setoptions](#),

*setoptions3d, spacecurve, sparsematrixplot, surfdata, textplot, textplot3d, tubeplot]*

*Digits := 20*

*c := 299792458*

*λ := 0.000001310*

*NumberOfLoops := 15*

*BendRadius := 0.015*

*SingleLoopWidth := 0.030*

*SingleLoopLength := 0.304*

*TotalArmLength := 4.560*

*TotalArmWidth := 0.450*

*TotalFiberLengthPerArm := 10.533716694115406957*

*Altitude :=  $\frac{23}{180} \pi$*

*vWind := 420000*

*v := 3.8661203845002493750 10<sup>5</sup>*

*n1 := 1.44915*

*n2 := 1.44975*

*n := 1.44975*

*γ := 1.0000008315337604908*

*cn := 2.0678907259872391792 10<sup>8</sup>*

*FractionOfTimeLightIsHeldByMolecules := 0.31022590101741679600*

*TimeLightIsHeldByMolecules := 1.5002057656243933286 10<sup>-9</sup> L*

*t0 := 4.8358454701352093386 10<sup>-9</sup> L*

*L1 :=  $\sqrt{L^2 + (3.8661203845002493750 10^5 dtDiagonal - 0.00057999760914252705320 L)^2}$*

*Eqdt0 := dtDiagonal = 1.5002045181536888428 10<sup>-9</sup> L*

*+  $\frac{1}{299792458}$*

*$\sqrt{L^2 + (3.8661203845002493750 10^5 dtDiagonal - 0.00057999760914252705320 L)^2}$*

*θ := θ*

*unitXcomponent :=  $|\cos(\theta)|^2$*

*unitYcomponent :=  $|\sin(\theta)|^2$*

*TotalArmLengthA := 4.560  $|\cos(\theta)|^2$*

*TotalArmWidthA := 0.450  $|\sin(\theta)|^2$*

*TotalArmLengthB := 4.560  $|\sin(\theta)|^2$*

*TotalArmWidthB := 0.450  $|\cos(\theta)|^2$*

*L := 4.560  $|\cos(\theta)|^2$*

*dtTotalArmLengthA := 2.2051467991870268162 10<sup>-8</sup>  $|\cos(\theta)|^2$*

$$\begin{aligned}
L &:= 0.450 |\sin(\theta)|^2 \\
dtTotalArmWidthA &:= 2.1761317097240396213 \cdot 10^{-9} |\sin(\theta)|^2 \\
L &:= 4.560 |\sin(\theta)|^2 \\
dtTotalArmLengthB &:= 2.2051467991870268162 \cdot 10^{-8} |\sin(\theta)|^2 \\
L &:= 0.450 |\cos(\theta)|^2 \\
dtTotalArmWidthB &:= 2.1761317097240396213 \cdot 10^{-9} |\cos(\theta)|^2 \\
dtPerpendicularArm1 &:= 4.4102935983740536324 \cdot 10^{-8} |\cos(\theta)|^2 \\
&+ 4.3522634194480792426 \cdot 10^{-9} |\sin(\theta)|^2 \\
dtPerpendicularArm2 &:= 4.4102935983740536324 \cdot 10^{-8} |\sin(\theta)|^2 \\
&+ 4.3522634194480792426 \cdot 10^{-9} |\cos(\theta)|^2 \\
L &:= L \\
TotalArmLengthContractedA &:= 4.5599962082092051640 |\sin(\theta)|^2 \\
TotalArmWidthContractedA &:= 0.44999962581011893066 |\cos(\theta)|^2 \\
TotalArmLengthContractedB &:= 4.5599962082092051640 |\cos(\theta)|^2 \\
TotalArmWidthContractedB &:= 0.44999962581011893066 |\sin(\theta)|^2 \\
dtParallelArm1 &:= 4.4102947360692281848 \cdot 10^{-8} |\sin(\theta)|^2 \\
&+ 4.3522645421735804455 \cdot 10^{-9} |\cos(\theta)|^2 \\
dtParallelArm2 &:= 4.4102947360692281848 \cdot 10^{-8} |\cos(\theta)|^2 \\
&+ 4.3522645421735804455 \cdot 10^{-9} |\sin(\theta)|^2 \\
dtArm1 &:= 4.8455200525914116770 \cdot 10^{-8} |\cos(\theta)|^2 + 4.8455210780140361091 \cdot 10^{-8} |\sin(\theta)|^2 \\
dtArm2 &:= 4.8455200525914116770 \cdot 10^{-8} |\sin(\theta)|^2 + 4.8455210780140361091 \cdot 10^{-8} |\cos(\theta)|^2 \\
dxArm1 &:= 14.526503668546685763 |\cos(\theta)|^2 + 14.526506742686376436 |\sin(\theta)|^2 \\
dxArm2 &:= 14.526503668546685763 |\sin(\theta)|^2 + 14.526506742686376436 |\cos(\theta)|^2 \\
d\theta_{arm1} &:= 1.5267175572519083969 \cdot 10^6 \left( 14.526503668546685763 |\cos(\theta)|^2 \right. \\
&\quad \left. + 14.526506742686376436 |\sin(\theta)|^2 \right) \pi \\
d\theta_{arm2} &:= 1.5267175572519083969 \cdot 10^6 \left( 14.526503668546685763 |\sin(\theta)|^2 \right. \\
&\quad \left. + 14.526506742686376436 |\cos(\theta)|^2 \right) \pi \\
LightIntensityEnvelope &:= -2 \sin \left( \right. \\
&\quad -1.5267175572519083969 \cdot 10^6 \left( 14.526503668546685763 |\cos(\theta)|^2 \right. \\
&\quad \left. + 14.526506742686376436 |\sin(\theta)|^2 \right) \pi \\
&\quad \left. + 1.5267175572519083969 \cdot 10^6 \left( 14.526503668546685763 |\sin(\theta)|^2 \right. \right.
\end{aligned}$$

$$+ 14.526506742686376436 |\cos(\theta)|^2 \pi)$$

$$WaveArm1 := \sin(1.5267175572519083969 \cdot 10^6 (14.526503668546685763 |\cos(\theta)|^2$$

$$+ 14.526506742686376436 |\sin(\theta)|^2) \pi)$$

$$WaveArm2 := \sin(1.5267175572519083969 \cdot 10^6 (14.526503668546685763 |\sin(\theta)|^2$$

$$+ 14.526506742686376436 |\cos(\theta)|^2) \pi)$$

$$LightIntensity := \sin(1.5267175572519083969 \cdot 10^6 (14.526503668546685763 |\cos(\theta)|^2$$

$$+ 14.526506742686376436 |\sin(\theta)|^2) \pi)$$

$$+ \sin(1.5267175572519083969 \cdot 10^6 (14.526503668546685763 |\sin(\theta)|^2$$

$$+ 14.526506742686376436 |\cos(\theta)|^2) \pi)$$

$$TimeDifference := 4.3696896470957918494 \cdot 10^{-15} Shift$$

$$dtEq := 4.3696896470957918494 \cdot 10^{-15} Shift = -1.0254226244321 \cdot 10^{-14} |\cos(\theta)|^2$$

$$+ 1.0254226244321 \cdot 10^{-14} |\sin(\theta)|^2$$

$$FringeShift := -2.3466715195977871229 |\cos(\theta)|^2 + 2.3466715195977871229 |\sin(\theta)|^2$$

*plot0 := PLOT(...)*

*plot1a := PLOT(...)*

*plot1b := PLOT(...)*

*plot2 := PLOT(...)*

*plot3 := PLOT(...)*

*plot4 := PLOT(...)*













