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> restart;

with(plots);

unprotect( $\gamma$ );

Digits := 50;

c := 299792458;

 $\lambda := \frac{c}{10.0E6}$ ;

NumberOfLoops := 1;
SingleLoopLength :=  $\frac{5}{2}$ ;

TotalArmLength := NumberOfLoops·SingleLoopLength;
Altitude :=  $0 \cdot \frac{\pi}{180}$ ;

Azimuth := 180;

vWind := 486000;

v := evalf(vWind·abs(cos(Altitude)));

# ArmA: Cable OUT is coaxial cable followed by single-mode optic fiber
#       Cable IN is single-mode optic fiber followed by coaxial cable

# ArmB: Cable OUT is single-mode optic fiber followed by coaxial cable
#       Cable IN is coaxial cable followed by single-mode optic fiber

n1 := 1.19;
n2 := 1.44975;

 $\theta := \frac{\pi}{4}$ ;
# X and Y components are equal as signal is traveling around a loop - so no changing  $\theta$ 

unitXcomponent := abs(cos( $\theta$ )2);

unitYcomponent := abs(sin( $\theta$ )2);

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$$\gamma := \text{evalf}\left(\frac{1}{\text{sqrt}\left(1 - \left(\frac{v}{c}\right)^2\right)}\right);$$

$$\text{FractionOfTimeLightIsHeldByMolecules} := \frac{(n - 1)}{n};$$

$$\text{TimeLightIsHeldByMolecules} := \gamma \cdot \text{FractionOfTimeLightIsHeldByMolecules} \cdot \frac{L \cdot n}{c};$$

$$\text{Eqdtn} := \text{dtDiagonal} = \gamma \cdot \text{TimeLightIsHeldByMolecules} + \frac{\gamma L}{c};$$

$$\text{EqdtnOptic} := \text{dtDiagonalOptic} = \text{TimeLightIsHeldByMolecules} + \frac{\gamma L}{c};$$

$$L := \text{unitXcomponent} \cdot \text{TotalArmLength};$$

$$n := n1; \quad \# \text{ Coaxial cable}$$

$$\text{dtTotalArmLengthAout} := \text{solve}(\text{Eqdtn}, \text{dtDiagonal});$$

$$n := n2; \quad \# \text{ Optic fiber}$$

$$\text{dtTotalArmLengthAin} := \text{solve}(\text{EqdtnOptic}, \text{dtDiagonalOptic});$$

$$n := n2; \quad \# \text{ Optic fiber}$$

$$\text{dtTotalArmLengthBout} := \text{solve}(\text{EqdtnOptic}, \text{dtDiagonalOptic});$$

$$n := n1; \quad \# \text{ Coaxial cable}$$

$$\text{dtTotalArmLengthBin} := \text{solve}(\text{Eqdtn}, \text{dtDiagonal});$$

$$\text{dtPerpendicularComponentArmA} := \text{dtTotalArmLengthAout} + \text{dtTotalArmLengthAin} \\ + \text{dtTotalArmLengthBout} + \text{dtTotalArmLengthBin};$$

$$\text{dtPerpendicularComponentArmB} := \text{dtTotalArmLengthBout} + \text{dtTotalArmLengthBin} \\ + \text{dtTotalArmLengthAout} + \text{dtTotalArmLengthAin};$$

$$L := 'L';$$

$$n := 'n';$$

$$\text{FractionOfTimeLightIsHeldByMoleculesUp} := \frac{(n - 1)}{n};$$

$$\text{TimeLightIsHeldByMoleculesInMovingFrameUp} := \text{FractionOfTimeLightIsHeldByMoleculesUp} \\ \cdot \frac{L \cdot n}{c};$$

$$\text{TimeLightIsHeldByMoleculesInAetherFrameUp} := \gamma \\ \cdot \text{TimeLightIsHeldByMoleculesInMovingFrameUp};$$

$$\text{opticalPathLengthUp} := \frac{L}{\gamma} + v \cdot dtup - v \cdot \text{TimeLightIsHeldByMoleculesInAetherFrameUp};$$

$$dtupEqn := dtup = \frac{\text{opticalPathLengthUp}}{c} + \text{TimeLightIsHeldByMoleculesInAetherFrameUp};$$

$$dtup := \text{solve}(dtupEqn, dtup);$$

$$\text{FractionOfTimeLightIsHeldByMoleculesDown} := \frac{(n - 1)}{n};$$

$$\text{TimeLightIsHeldByMoleculesInMovingFrameDown} \\ := \text{FractionOfTimeLightIsHeldByMoleculesDown} \cdot \frac{L \cdot n}{c};$$

$$\text{TimeLightIsHeldByMoleculesInAetherFrameDown} := \gamma \\ \cdot \text{TimeLightIsHeldByMoleculesInMovingFrameDown};$$

$$\text{opticalPathLengthDown} := \frac{L}{\gamma} - v \cdot dtdown + v \\ \cdot \text{TimeLightIsHeldByMoleculesInAetherFrameDown};$$

$$dtdownEqn := dtdown = \frac{\text{opticalPathLengthDown}}{c} \\ + \text{TimeLightIsHeldByMoleculesInAetherFrameDown};$$

$$dtdown := \text{solve}(dtdownEqn, dtdown);$$

$$L := \text{unitYcomponent} \cdot \text{TotalArmLength};$$

$$n := n1; \quad \# \text{ Coaxial cable}$$

$$dtArmAout := dtup;$$

$$n := n2; \quad \# \text{ Optic fiber}$$

$$dtArmAin := dtdown;$$

$L := \text{unitYcomponent} \cdot \text{TotalArmLength};$

$n := n2; \quad \# \text{ Optic fiber}$

$dtArmBout := dtup;$

$n := n1; \quad \# \text{ Coaxial cable}$

$dtArmBin := dtdown;$

$dtParallelComponentArmA := dtArmAout + dtArmAin + dtArmBout + dtArmBin;$

$dtParallelComponentArmB := dtArmBout + dtArmBin + dtArmAout + dtArmAin;$

$dtArmA := \frac{1}{\gamma} \cdot (dtPerpendicularComponentArmA + dtParallelComponentArmA);$

$dtArmB := \frac{1}{\gamma} \cdot (dtPerpendicularComponentArmB + dtParallelComponentArmB);$

$L := 'L';$

$Lcontracted := 'Lcontracted';$

$v := 'v';$

$n := 'n';$

$TimeDifference := \frac{Shift \cdot \lambda}{c};$

$dtDiff := dtArmA - dtArmB;$

$dtSum := dtArmA + dtArmB;$

$dtEq := TimeDifference = dtSum;$

$FringeShift := \text{evalf}(\text{solve}(dtEq, Shift));$

$dtArmAresult := \text{evalf}(dtArmA \cdot 1E12);$

$dtArmBresult := \text{evalf}(dtArmB \cdot 1E12);$

$dtDiffResult := \text{evalf}(dtDiff \cdot 1E12);$

$dtSumResult := \text{evalf}(dtSum \cdot 1E12);$

$FringeShift := \text{evalf}(FringeShift);$

$FringeShiftDistanceResult := \text{evalf}(FringeShift \cdot \lambda);$

$MaximumTimeDifferenceInPicosecondsOnRotation := dtSumResult;$



$$dtTotalArmLengthAout := 4.9617734769198289559682269331484456654250052632755 \cdot 10^{-9}$$

$$n := 1.44975$$

$$dtTotalArmLengthAin := 6.0448147806664138897582092460898066950680379765138 \cdot 10^{-9}$$

$$n := 1.44975$$

$$dtTotalArmLengthBout := 6.0448147806664138897582092460898066950680379765138 \cdot 10^{-9}$$

$$n := 1.19$$

$$dtTotalArmLengthBin := 4.9617734769198289559682269331484456654250052632755 \cdot 10^{-9}$$

$$dtPerpendicularComponentArmA :=$$

$$2.2013176515172485691452872358476504720986086479578 \cdot 10^{-8}$$

$$dtPerpendicularComponentArmB :=$$

$$2.2013176515172485691452872358476504720986086479578 \cdot 10^{-8}$$

$$L := L$$

$$n := n$$

$$FractionOfTimeLightIsHeldByMoleculesUp := \frac{n-1}{n}$$

$$TimeLightIsHeldByMoleculesInMovingFrameUp := \frac{1}{299792458} (n-1) L$$

$$TimeLightIsHeldByMoleculesInAetherFrameUp :=$$

$$3.3356453350806215635844575939795449946917954000421 \cdot 10^{-9} (n-1) L$$

$$opticalPathLengthUp := 0.99999868598167347971648838783612394919328641647623 L$$

$$+ 4.86000 \cdot 10^5 dtup$$

$$- 0.0016211236328491820799020463906740588674202125644205 (n-1) L$$

$$dtupEqn := dtup = 3.3356365688881789004728344027791517997203465888266 \cdot 10^{-9} L$$

$$+ 0.0016211215026630189609373028323481039673119461864514 dtup$$

$$+ 3.3302378487026647769600854545354164206920445038257 \cdot 10^{-9} (n-1) L$$

$$dtup := 5.4074863779567866243721394441285739997508962166955 \cdot 10^{-12} L$$

$$+ 3.3356453350806215635844575939795449946917954000421 \cdot 10^{-9} L n$$

$$FractionOfTimeLightIsHeldByMoleculesDown := \frac{n-1}{n}$$

$$TimeLightIsHeldByMoleculesInMovingFrameDown := \frac{1}{299792458} (n-1) L$$

$$TimeLightIsHeldByMoleculesInAetherFrameDown :=$$

$$3.3356453350806215635844575939795449946917954000421 \cdot 10^{-9} (n-1) L$$

$$opticalPathLengthDown := 0.99999868598167347971648838783612394919328641647623 L$$

$$- 4.86000 \cdot 10^5 dtdown$$

$$+ 0.0016211236328491820799020463906740588674202125644205 (n-1) L$$

$$dtdownEqn := dtdown = 3.3356365688881789004728344027791517997203465888266 \cdot 10^{-9} L$$

$$- 0.0016211215026630189609373028323481039673119461864514 dtdown$$

$$+ 3.3410528214585783502088297334236735686915462962585 \cdot 10^{-9} (n-1) L$$

